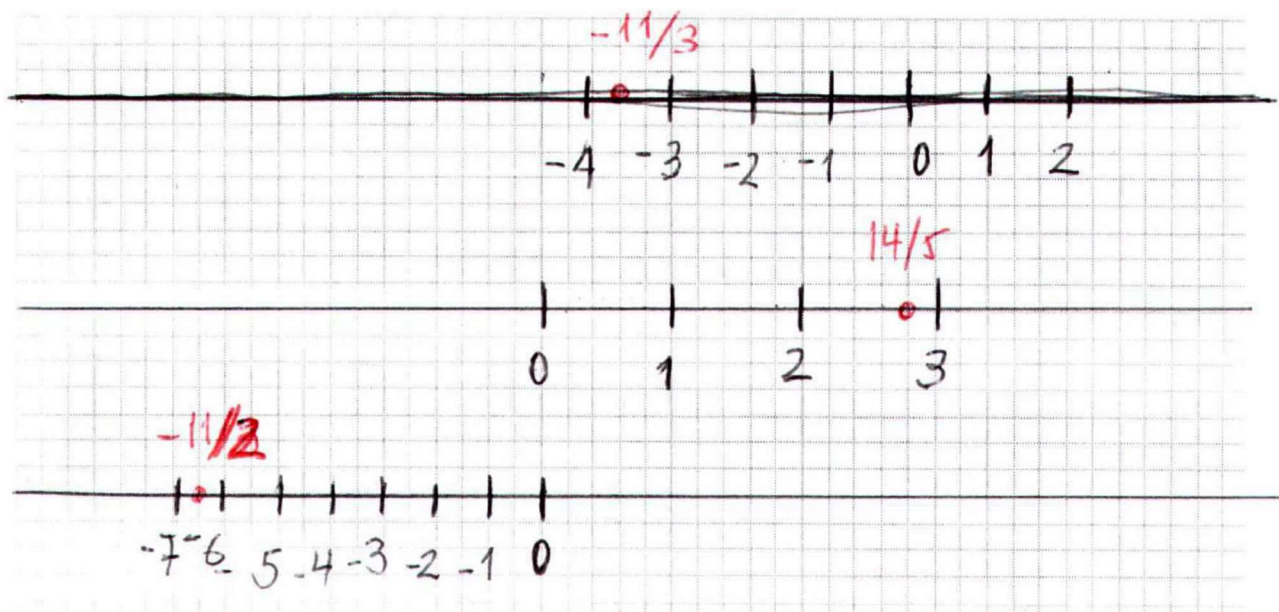


**Lesson 07 and 08: Fractions and fraction operations. AD**

1. Represent the following fractions on the number line: a)  $-\frac{11}{3}$ ; b)  $\frac{14}{5}$ ; c)  $-\frac{13}{2}$ . You can draw a line for each fraction:



2. Get the resulting simplest fraction:  $\frac{1}{4} : \left[ \frac{3}{4} - 3 \cdot \left( 2 - \frac{8}{5} \right) \right]$

$$= \frac{1}{4} : \left[ \frac{3}{4} - 3 \cdot \left( \frac{10}{5} - \frac{8}{5} \right) \right] = \frac{1}{4} : \left[ \frac{3}{4} - 3 \cdot \frac{2}{5} \right] =$$

$$= \frac{1}{4} : \left[ \frac{3}{4} - \frac{6}{5} \right] = \frac{1}{4} : \left[ \frac{15}{20} - \frac{24}{20} \right] =$$

$$= \frac{1}{4} : \left[ -\frac{9}{20} \right] = -\frac{20}{36} = -\frac{10}{18} = \boxed{-\frac{5}{9}}$$

Surname and name \_\_\_\_\_



3. This is a table that gathers the information about the effectiveness of four basketball players. Order the players by their effectiveness.

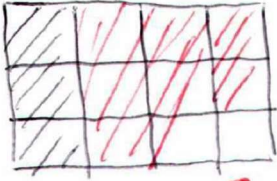
Player	A	B	C	D
Field goals	4	5	8	6
Throws	6	8	15	10

$$\begin{array}{l}
 A: \frac{4}{6} = \frac{80}{120} \\
 B: \frac{5}{8} = \frac{75}{120} \\
 C: \frac{8}{15} = \frac{64}{120} \\
 D: \frac{6}{10} = \frac{72}{120}
 \end{array}
 \left. \vphantom{\begin{array}{l} A \\ B \\ C \\ D \end{array}} \right\} C < D < B < A$$

$$\begin{array}{cccc}
 6 \overline{) 2} & 8 \overline{) 2} & 15 \overline{) 3} & 10 \overline{) 2} \\
 3 \overline{) 3} & 4 \overline{) 2} & 5 \overline{) 5} & 5 \overline{) 5} \\
 1 & 2 & 1 & 1 \\
 2.3 & 2.3 & 3.5 & 2.5 \\
 \text{m.c.m.} = 2^3 \cdot 3 \cdot 5 = 120
 \end{array}$$

4. A tap fills  $\frac{1}{4}$  of a tank in an hour and another fills  $\frac{2}{3}$  of it in an hour.

- Draw the tank and the filled part by each tap. You can draw two different pictures, one for each.
- What part do they fill in an hour together?
- What portion is empty after an hour?
- If the tank is 2400 litres of capacity, what is the volume of the empty part?

a) 

b)  $\frac{1}{4} + \frac{2}{3} = \frac{3}{12} + \frac{8}{12} = \frac{11}{12}$

c)  $\frac{12}{12} - \frac{11}{12} = \frac{1}{12}$

d)  $\frac{1}{12} \cdot 2400 = \frac{2400}{12} = 200 \text{ l}$



5. Convert these mixed numerals to improper fraction form:

a)  $2\frac{5}{8}$

b)  $3\frac{4}{5}$

Convert these fractions to mixed numeral form:

c)  $\frac{12}{5}$

d)  $\frac{37}{8}$

a)  $2\frac{5}{8} = \boxed{\frac{21}{8}}$  ; b)  $3\frac{4}{5} = \boxed{\frac{19}{5}}$

c)  $\frac{12}{5} = \boxed{2\frac{2}{5}}$  ;  $\frac{37}{8} = \boxed{4\frac{5}{8}}$

$\frac{12}{5} = \frac{12 \cdot 2}{5 \cdot 2} = \frac{24}{10} = \frac{12}{5}$

$\frac{37}{8} = \frac{37 \cdot 4}{8 \cdot 4} = \frac{148}{32} = \frac{37}{8}$

6. a) What do you have to do to compare fractions?

We can do it in two different ways:

1) To get the decimal value

2) To reduce to common denominator

b) What is the letter we use to represent rational numbers?

$\mathbb{Q}$

e) What is an improper fraction? Write an example.

It is a fraction whose denominator is greater than the numerator.



d) What is the order of the operations?

1<sup>st</sup>: Parentheses  
 2<sup>nd</sup>: Powers and roots  
 3<sup>rd</sup>: Products and divisions  
 4<sup>th</sup>: Sums and subtractions.

7. Get the resulting fraction:  $\frac{\frac{3}{5} - 7}{\frac{2}{3} + \frac{4}{5}} - \frac{2}{5 - \frac{7}{3}} =$

$$\begin{aligned}
 & \frac{\frac{3}{5} - 7}{\frac{2}{3} + \frac{4}{5}} - \frac{2}{5 - \frac{7}{3}} = \\
 & \frac{\frac{3}{5} - \frac{35}{5}}{\frac{10}{15} + \frac{12}{15}} - \frac{2}{\frac{15}{3} - \frac{7}{3}} = \frac{-\frac{32}{5}}{\frac{22}{15}} - \frac{2}{\frac{8}{3}} = \\
 & = -\frac{32 \cdot 15}{5 \cdot 22} - \frac{2 \cdot 3}{8 \cdot 1} = -\frac{480}{110} - \frac{6}{8} = \\
 & = \frac{-48}{11} - \frac{3}{4} = \frac{-192}{44} - \frac{33}{44} = \boxed{\frac{-225}{44}}
 \end{aligned}$$

Surname and name \_\_\_\_\_



8. Calculate the decimal value for the following fractions and classify them according to the result. Include the operation to get the decimal expression for each.

a) $\frac{59}{6} =$	b) $\frac{117}{13} =$	c) $\frac{27}{8} =$
$a) \frac{59}{6} = 9\overline{83}$ repeating decimal <div style="text-align: right;"> <math display="block">\begin{array}{r} 59 \overline{) 6} \\ \underline{50} \phantom{00} \\ 20 \phantom{00} \\ \underline{18} \phantom{00} \\ 2 \phantom{00} \end{array}</math> </div>	$b) \frac{117}{13} = 9$ Integer <div style="text-align: right;"> <math display="block">\begin{array}{r} 117 \overline{) 13} \\ \underline{00} \phantom{00} \\ 9 \phantom{00} \end{array}</math> </div>	$c) \frac{27}{8} = 3\overline{375}$ finite decimal <div style="text-align: right;"> <math display="block">\begin{array}{r} 27 \overline{) 18} \\ \underline{30} \phantom{00} \\ 60 \phantom{00} \\ \underline{40} \phantom{00} \\ 20 \phantom{00} \\ \underline{18} \phantom{00} \\ 2 \phantom{00} \end{array}</math> </div>

9. Convert the following decimal numbers into a fraction in simplest form; that is, you must reduce the fraction as much as possible.

a)  $-2\frac{1}{5}$ ; b)  $20\frac{1}{4}$ ; c)  $-0\frac{6}{100}$

$$a) -2\frac{1}{5} = \frac{-25}{10} = \boxed{\frac{-5}{2}}$$

$$b) 20\frac{1}{4} = \frac{204}{10} = \boxed{\frac{102}{5}}$$

$$c) -0\frac{6}{100} = \frac{-6}{100} = \boxed{\frac{-3}{50}}$$

10. Calculate the following powers:

a)  $\left(\frac{3}{5}\right)^3$ ; b)  $\left(\frac{-2}{7}\right)^2$

$$a) \left(\frac{3}{5}\right)^3 = \left(\frac{3}{5}\right)\left(\frac{3}{5}\right)\left(\frac{3}{5}\right) = \frac{27}{125}$$

$$b) \left(\frac{-2}{7}\right)^2 = \left(\frac{-2}{7}\right)\left(\frac{-2}{7}\right) = \frac{4}{49}$$